	th Class 2015	Jan all
Math (Science)	Group-I	D
Time: 2.10 Hours	(Subjective Type)	Max. Marks: 6
	(Part-I)	3.60

Write short answers to any Six (6) questions: 12 2.

(i) Find |C|:
$$C = \begin{bmatrix} 3 & 2 \\ 3 & 2 \end{bmatrix}$$

Ans $C = \begin{bmatrix} 3 & 2 \\ 3 & 2 \end{bmatrix}$

$$|C| = \begin{bmatrix} 3 & 2 \\ 3 & 2 \end{bmatrix}$$

$$|C| = (3)(2) - 3(2)$$

$$|C| = 6 - 6$$

$$|C| = 0$$

(ii) Find the product:
$$\begin{bmatrix} 1 & 2 \\ -3 & 0 \\ 6 & -1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 0 & -4 \end{bmatrix}$$
Ans
$$\begin{bmatrix} 1 & 2 \\ -3 & 0 \\ 6 & -1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 0 & -4 \end{bmatrix}$$

Ans
$$\begin{bmatrix} 1 & 2 \\ -3 & 0 \\ 6 & -1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 0 & -4 \end{bmatrix}$$

1st matrix has (3 × 2) order, while 2nd matrix has (2) order. As number of columns of 1st matrix is equal number of rows of 2nd matrix, thus product of about matrices will exist. So,

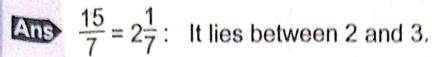
$$\begin{bmatrix}
1 & 2 \\
-3 & 0 \\
6 & -1
\end{bmatrix}
\begin{bmatrix}
4 & 5 \\
0 & -4
\end{bmatrix}$$

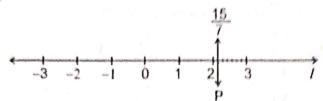
$$= \begin{bmatrix}
1(4) + 2(0) & 1(5) + 2(-4) \\
-3(4) + 0(0) & -3(5) + 0(-4) \\
6(4) + (-1)(0) & 6(5) + (-1)(-4)
\end{bmatrix}$$

$$= \begin{bmatrix}
4 + 0 & 5 - 8 \\
-12 + 0 & -15 + 0 \\
24 + 0 & 30 + 4
\end{bmatrix}$$

$$=\begin{bmatrix} 4 & -3 \\ -12 & -15 \\ 24 & 34 \end{bmatrix}$$

(iii) Represent the number $\frac{15}{7}$ on the number line.





Divide the distance between 2 and 3 into seven equal parts. The point P represents the number $\frac{15}{7} = 2\frac{1}{7}$.

(iv) Write the real and imaginary part of the number: 2 + 0i:

(v) Write into sum or difference: $\log \frac{(22)^{1/3}}{5^3}$

$$\log \frac{(22)^{1/3}}{5^3}$$

$$= \log (22)^{1/3} - \log (5)^3$$

$$= \frac{1}{3} \log (22) - 3 \log (5)$$

vi) Write in the form of a single logarithm:

$$\log 25 - 2 \log 3$$

log 25 – 2 log 3
= log 25 – log 3²
=
$$\frac{\log 25}{\log 3^2} = \log \frac{25}{3^2}$$

vii) Reduce the algebraic fraction to their lowest form: $\frac{lx + mx - ly - my}{3x^2 - 3v^2}$

Ans
$$\frac{lx + mx - ly - my}{3x^2 - 3y^2} = \frac{x(l + m) - y(l + m)}{3(x^2 - y^2)}$$

$$= \frac{(l+m)(x-y)}{3(x+y)(x-y)}$$
 (Factorizing)
= $\frac{l+m}{3(x+y)}$ (Canceling common factors)
Which is in the lowest form.

(viii) Evaluate
$$\frac{x^2y-2z}{xz}$$
 for $x=3$, $y=-1$, $z=-2$

By putting the values x = 3, y = -1, z = -2 in the expression $\frac{x^2y - 2z}{xz}$:

$$= \frac{(3)^{2}(-1) - (2)(-2)}{(3)(-2)}$$

$$= \frac{9(-1) + 4}{-6}$$

$$= \frac{-9 + 4}{-6}$$

$$= \frac{-5}{-6}$$

(ix) Define remainder theorem.

If a polynomial p(x) is divided by a linear divisor (x-1) then the remainder is p(a).

- 3. Write short answers to any Six (6) questions:
- (i) Find square root of the following $4x^2 12x + 9$ by factorization Factorization of the expression $4x^2 12x + 9$ the type: $(a)^2 2(a)(b) + (b)^2 = (a b)^2$

So,
$$4x^2 - 12x + 9$$

= $(2x)^2 - 2(2x)(3) + (3)^2$
= $(2x - 3)^2$

Taking square root

$$= \pm (2x - 3)$$

(ii) Solve it: $\sqrt[3]{2x-4}-2=0$ Ans $\sqrt[3]{2x-4}=2$

$$(2x - 4)^{1/3} = 2$$

By taking cube both sides,
 $[(2x - 4)^{1/3}]^3 = (2)^3$
 $2x - 4 = 8$
 $2x = 8 + 4$
 $2x = 12$
 $x = \frac{12}{2}$

Find the solution set of the equation: $\left| \frac{x+5}{2-x} \right| = 6$ (iii)

Ans

$$\left| \frac{x+5}{2-x} \right| = 6$$

$$\pm \left(\frac{x+5}{2-x} \right) = 6$$

$$\frac{x+5}{2-x} = 6$$

$$x+5 = 6(2-x)$$

$$x+5 = 12-6x$$

$$x+6x = 12-5$$

$$7x = 7$$

$$x = \frac{7}{7}$$

$$\frac{x+5}{2-x} = 6$$

$$x+5 = 6(2-x)$$

$$x+5 = 12-6x$$

$$x+6x = 12-5$$

$$7x = 7$$

$$x = \frac{7}{7}$$

$$x = \frac{7}{7}$$

$$x = 1$$

$$x = \frac{17}{5}$$

$$x = \frac{17}{5}$$

So, solution set = $\left\{1, \frac{17}{5}\right\}$

Define Cartesian Plane. (iv)

Ans The Cartesian plane establishes (one-to-one) correspondence between the set of ordered pairs $R \times R =$ $\{(x, y) \mid x, y \in R\}$ and the points of the Cartesian plane.

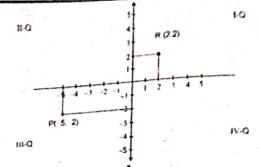
Draw in which quadrant points lie P(-5, -2), R(2, 2). (V)

Ans

Ordered Pair P(-5, -2)R(2, 2)

Quadrant

$$III - Q$$
$$I - Q$$



(vi) Define equilateral triangle.

If the lengths of all the three sides of a triangle a same, then the triangle is called an equilateral triangle.

(vii) Find the distance between points

$$A(-4, \sqrt{2}), B(-4, -3)$$

Formula for distance between two points:

$$d = \sqrt{|x_2 - x_1|^2 + |y_2 - y_1|^2}$$

Here, from question:

$$x_1 = -4$$
 , $y_1 = \sqrt{2}$
 $x_2 = -4$, $y_2 = -3$

By putting, we get:

$$d = \sqrt{[(-4) - (-4)]^2 + [(-3) - \sqrt{2}]^2}$$

$$d = \sqrt{(-4 + 4)^2 + (-3 - \sqrt{2})^2}$$

$$d = \sqrt{0 + [(-1)(3 + \sqrt{2})]^2}$$

$$d = \sqrt{(-1)^2(3 + \sqrt{2})^2}$$

$$d = \sqrt{(3 + \sqrt{2})^2}$$

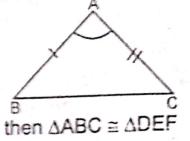
$$d = 3 + \sqrt{2}$$

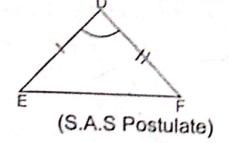
(viii) What do you mean by SAS ≅ SAS?

In any correspondence of two triangles, if two sides and their included angle of one triangle are congruent the corresponding two sides and their included angle the other, then the triangles are congruent.

In $\triangle ABC \longleftrightarrow \triangle DEF$, shown in the following figures

if
$$\begin{cases} \overline{AB} \cong \overline{DE} \\ \angle A \cong \angle D \end{cases}$$
$$\overline{AC} \cong \overline{DF}$$





(ix) Define parallelogram.

Ans A figure formed by four non-collinear points in the plane is called parallelogram. It characteristics are as under:

- Its equal opposite sides are of equal measure.
- Its opposite sides are parallel.
- Measure of none of the angle is 90°.

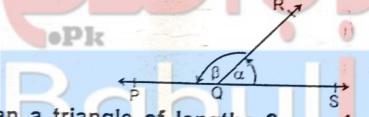
4. Write short answers to any Six (6) questions: 12

(i) Define supplementary angles. Give an example.

Supplementary angles are two angles whose sum is 180°. If the sum of two angles is 180°, then each angle is called the supplement of the other.

For example, in the following figure, $\angle \alpha$ and $\angle \beta$ are

supplementary angles.



(ii) Can a triangle of lengths 2 cm, 4 cm and 7 cm be formed? Give reason.

2 cm, 4 cm and 7 cm cannot be the sides of a triangles, because 2 + 4 < 7. The condition for forming a triangle is the sum of the lengths of any two sides of a triangle is greater than the length of the third side.

(iii) Define proportion.

Equality of two ratios is defined as the proportion. If a: b = c: d, then a, b, c and d are said to be a proportion.

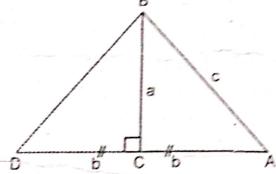
(iv) Define similar triangles.

Two (or more) triangles are called similar, if they are equiangular and measure of their corresponding sides are proportional. The symbol for similar triangle is (~).

(v) What is meant by converse of Pythagoras theorem:

Converse of Pythagoras theorem is:

If the square of one side of a triangle is equal to sum of the squares of the other two sides, then triangle is a right angled triangle.



(vi) Find the value of unknown x:



Ans in right angled ΔABC is:

 $(m AC)^2 = (m AB)^2 + (m BC)^2$ (Pythagoras Theorem By putting values:

$$(\sqrt{2})^2 = (x)^2 + (1)^2$$

 $2 = x^2 + 1$
 $x^2 = 2 - 1$
 $x^2 = 1$
By taking square root:

$$\sqrt{x^2} = \sqrt{1}$$
$$x = 1 \text{ cm}$$

(vii) Define triangular region.

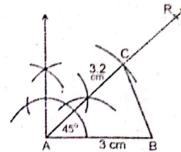
Ans A triangular region is the union of a triangle and interior, i.e., the three line segments forming the triangle and its interior.

(viii) Define circumcentre of a triangle.

The point of concurrency of the perpendicular bisectors of the sides of a triangle is called its circumcents

(ix) Construct △ ABC, in which: m AB = 3 cm, m AC = 3 cm, m∠ A = 45°





Steps of Construction:

- Take a line segment $\overline{AB} = 3$ cm.
- i) Make an angle of 45° at A.
- ii) Take A as centre and cut off $\overrightarrow{AC} = 3.2$ cm on \overrightarrow{AR} .
- v) Join C to B.
- (v) ABC is the required triangle.

(Part-II)

IOTE: Attempt Three (3) questions in all. But question No. 9 is Compulsory.

Q.5.(a) Solve with help of Cramer's rule:

(4)

$$4x + 2y = 8$$

$$3x - y = -1$$

Write the equations in matrix form

$$\begin{bmatrix} 4 & 2 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$

Let, AX = BWhere,

$$A = \begin{bmatrix} 4 & 2 \\ 3 & -1 \end{bmatrix}, X = \begin{bmatrix} x \\ y \end{bmatrix}, B = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$

$$|A| = \begin{vmatrix} 4 & 2 \\ 3 & -1 \end{vmatrix}$$

$$|A| = (4)(-1) - (2)(3)$$

$$|A| = -4 - 6$$

$$|A| = -10$$

$$|A| = \begin{vmatrix} 8 & 2 \\ -1 & -1 \end{vmatrix}$$

$$|A_i| = (8)(-1) - (-1)(2)$$

$$|A_i| = -8 + 2$$

$$|A_i| = -6$$

$$|A_i| = |A_i| = |A$$

(4)Q.6.(a) Use log tables to find the value of: $\frac{(438)^3 \sqrt{0.056}}{(388)^4}$ $x = \frac{(438)^3 \sqrt{0.056}}{(388)^4}$ Let $x = \frac{(438)^3 (0.056)^{1/2}}{(388)^4}$ By taking log, both sides: $\log x = \log \left[\frac{(438)^3 (0.056)^{1/2}}{(388)^4} \right]$ $\log x = 3 \log 438 + \frac{1}{2} \log 0.056 - 4 \log 388$ $\log x = 3(2.6415) + \frac{1}{2}(\overline{2}.7482) - 4(2.5888)$ $\log x = 7.9245 + \overline{1} \cdot 3741 - 10.3552$ $\log x = 7.9245 - 1 + 0.3741 - 10.3552$ $\log x = -3.0566$ $\log x = -3.0566 - 1 + 1$ $\log x = \bar{4} \cdot 9434$ Taking antilog both sides, x = Antilog (4.9434)x = 0.0008778 $\frac{\sqrt{a^2+2}+\sqrt{a^2-2}}{\sqrt{a^2+2}-\sqrt{a^2-2}}$ Simplify: (b) (4)With Rationalization: Ans $= \frac{\sqrt{a^2 + 2} + \sqrt{a^2 - 2}}{\sqrt{a^2 + 2} - \sqrt{a^2 - 2}} \times \frac{\sqrt{a^2 + 2} + \sqrt{a^2 - 2}}{\sqrt{a^2 + 2} + \sqrt{a^2 - 2}}$ $= \frac{(\sqrt{a^2+2})^2 + (\sqrt{a^2-2})^2 + 2(\sqrt{a^2+2})(\sqrt{a^2-2})}{(a^2+2) - (a^2-2)}$

$$= \frac{(a^2 + 2) + (a^2 - 2) + 2\sqrt{(a^2 + 2)(a^2 - 2)}}{a^2 + 2 - a^2 + 2}$$

$$= \frac{a^2 + 2 + a^2 - 2 + 2\sqrt{(a^2)^2 - (2)^2}}{4}$$

$$= \frac{2a^2 + 2\sqrt{a^4 - 4}}{4}$$

$$= \frac{2(a^2 + \sqrt{a^4 - 4})}{4}$$

$$= \frac{a^2 + \sqrt{a^4 - 4}}{2}$$

2.7.(a) Factorize: $2x^3 + x^2 - 2x - 1$

We have; $P(x) = 2x^3 + x^2 - 2x - 1$ The possible factors of the constant term

$$P = -1$$
 are ± 1 , $\pm \frac{1}{2}$.

From factors of the constant

Let,
$$x = -1$$

 $P(-1) = 2(-1)^3 + (-1)^2 - 2(-1) - 1$
 $= 2(-1) + 1 + 2 - 1$
 $= -2 + 3 - 1$

Hence, x = -1 is a zero of P(x);

As,
$$x-a=0$$

 $x-(-1)=0$
 $x+1=0$

So, x + 1 is the 1st factor of P(x). Similarly,

Let
$$x = 1$$

P(1) = $2(1)^3 + (1)^2 - 2(1) - 1$
= $2(1) + 1 - 2 - 1$
= $2 + 1 - 2 - 1$
= 0

Hence, x = 1 is a zero of P(x); As, x - a = 0

$$x - 1 = 0$$

So, x - 1 is the 2^{nd} factor of P(x).

Again;

Let
$$x = \frac{-1}{2}$$

$$P(\frac{-1}{2}) = 2(\frac{-1}{2})^3 + (\frac{-1}{2})^2 - 2(\frac{-1}{2}) - 1$$

$$= 2(\frac{-1}{8}) + (\frac{1}{4}) + 1 - 1$$

$$= \frac{-1}{4} + \frac{1}{4} + 0$$

$$= 0$$

Hence, $x = \frac{-1}{2}$ is a zero of P(x)

As,
$$x - a = 0$$

 $x - (\frac{-1}{2}) = 0$

Plx +
$$\frac{1}{2}$$
 = 0

$$(2)(x) + (2)(\frac{1}{2}) = (0)(2)$$

$$2x + 1 = 0$$

So, 2x + 1 is the last factor of P(x). As from the expression, there exist maximum three factors, i.e.,

The factors of P(x) are = (x - 1)(x + 1)(2x + 1)

(b) Find the H.C.F of the following polynomials: (4) $x^2 - 4$, $x^2 + 4x + 4$, $2x^2 + x - 6$

Ans By factorization:

$$x^{2}-4 = (x + 2)(x - 2)$$

 $x^{2}+4x+4 = (x + 2)^{2} = (x + 2)(x + 2)$
 $2x^{2}+x-6 = 2x^{2}+4x-3x-6$
 $= 2x(x + 2) - 3(x + 2)$
 $= (x + 2) (2x - 3)$
Hence, H.C.F = x + 2

$$|8x - 3| = |4x + 5|$$

 $8x - 3 = \pm(4x + 5)$

Since two numbers having the same absolute are either equal or differ in sign, therefore, the given equation is equivalent to

$$8x - 3 = 4x + 5$$

 $8x - 4x = 5 + 3$
 $4x = 8$
 $x = 2$

$$8x - 3 = -(4x + 5)$$

$$8x - 3 = -4x - 5$$

$$8x + 4x = -5 + 3$$

$$12x = -2$$

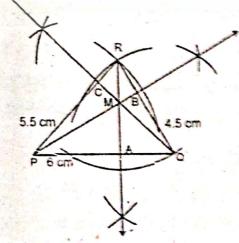
$$x = -\frac{1}{6}$$

On checking, we find that x = 2, $x = \frac{-1}{6}$ both satisfies the original equation.

Hence the solution set =
$$\left\{\frac{-1}{6}, 2\right\}$$
.

(b) Construct ΔPQR, draw its altitudes and show that they are concurrent:

$$m\overline{PQ} = 6 \text{ cm}, m\overline{QR} = 4.5 \text{ cm} \text{ and } m\overline{PR} = 5.5 \text{ cm}$$



Steps of Construction:

- (i) Take a line segment PQ = 6 cm.
- (ii) Take P as centre and draw an arc of 5.5 radius.
- (iii) Take Q as centre and draw an arc of 4.5 radius.

v) Join R to P and Q.

PQR is the required triangle.

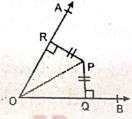
v) Drop RA, PB and QC perpendiculars to PQ, QR and RP, respectively.

RA, PB and QC are concurrent at M.

Q.9. Prove that any point inside an angle, equidistant from its arms, is on the bisector of it. (8)

Ans Given:

Any point P lies inside $\angle AOB$ such that $\overrightarrow{PQ} \cong \overrightarrow{PR}$, where $\overrightarrow{PQ} \perp \overrightarrow{OB}$ and $\overrightarrow{PR} \perp \overrightarrow{OA}$.



To Prove:

Point P is on the bisector of ∠AOB.

Construction:

Join P to O.

Proof:

In

Statements

ΔPOQ ↔ ΔPOR ∠PQO ≅ ∠PRO

PO = PO

PQ = PR

ΔPOQ ≅ ΔPOR

Hence, ∠POQ ≅ ∠POR

i.e., P is on the bisector of ∠AOB.

Reasons

given (right angles)
common

given

H.S ≅ H.S

(corresponding angles of congruent triangles)

OR

Prove that triangles on the same base and of the same (i.e., equal) altitudes are equal in area.

For Answer see Paper 2014 (Group-I), Q.9.(OR).